# MATH 353: Engineering Mathematics III - Section 012 

Spring 2013 (F.-J. Sayas)
Homework \#2
Due February 22

Instructions. The coding part of the exercises has to be turned in as Matlab output (copypaste from the Matlab window and/or editor). You can try and figure out how to use the Matlab Publish utility. (Google it!). Bring the homework to Friday's lecture. (That's collecting point and time. If you cannot make it, give it to someone else. If you cannot make that either, tell me in advance (no late homework!) and we'll make it work.)

1. Write an anonymous Matlab function corresponding to

$$
f(x)=\frac{\cos \left(10 x^{2}\right)}{1+x^{2}}
$$

and plot it in $[-4,4]$, using plot and fplot. Give the instructions you had to use to produce the plots. I care more about the commands than about the plot itself.
2. Write the mathematical expression for the following function

$$
f=@(x) x \cdot \wedge 2 \cdot *(x>0) . *(x<1)+(1+x) \cdot \wedge 2 \cdot *(x>=1) ;
$$

3. We now create the list
```
list = 1:0.1:2;
```

How many element does the array list have? Find out what the following quantities are

```
list(3) list(3:5) list(1:2:end)
```

You should be able to figure it out before you type the question to get the result.
4. Write an algorithmic description (that is, write the iteration with mathematically meaningful formulas) of the following iterative process:

```
x=1;
for i=1:2e+2
    x=0.5*(x+3/x);
end
```

(I'm asking also how many iterations you get to do when you run this piece of code.)
5. Just run the code. Use the code bisection.m to find the root to six correct decimal places of the following equations

$$
x^{3}=9 \quad \text { and } \quad \cos ^{2} x+6=x
$$

(You will first need to figure out an interval where you can gurantee the algorithm to find a solution.)
6. Programming exercise. You are going now to build an m-file babylonian.m containing specifically designed code for the following iteration

$$
x_{0}=a, \quad x_{i+1}=\frac{1}{2}\left(x_{i}+\frac{a}{x_{i}}\right) \quad i=1, \ldots, i \operatorname{tmax}
$$

Here $a>0$ is a parameter. (By specifically designed, I mean that the code has to solve this problem and nothing else. Do not use the general code of fixed point iteration for this.)

- Show (with math) that if this iteration converges, it converges to $\sqrt{a}$.
- Show that $x_{i}>0$ for all $i$.
- Prepare a function with following prototype

```
function [sqa,err]=babylonian(a,itmax)
```

- The output is sqa, the approximation of $\sqrt{a}$ after itmax iterations, and an array err with the quantities $\left|x_{i}-\sqrt{a}\right|$.
- Run it for $a=3$ and check your result.

Read about this method in your book.(Example 1.6.)
7. A mathematically tricky question. A continuously differentiable function $g$ has exactly three fixed points $r=1, r=2$ and $r=3$. We know that $g^{\prime}(1)=g^{\prime}(3)=\frac{1}{2}$. Show that $g^{\prime}(2)>1$. The argument can be made with a correctly drawn graph, by understanding what fixed points are and what a derivative means.

