MATH 612: CM4ES&FM

Spring'14

Homework # 5

Due May 12

Instructions

- The Assignment 2 and 3 problems make reference to problems at the end of the classnotes we have been using for the optimization part.
- One problem per page. (You can have two problems in different sides of the same page.)
- The fourth requires some coding. This problem has to be solved individually.
- 1. Show that if f_1, \ldots, f_k is convex and $\lambda_1, \ldots, \lambda_k \ge 0$, then $g = \lambda_1 f_1 + \ldots + \lambda_k f_k$ is convex. Show that if in addition f_1 is strictly convex and $\lambda_1 > 0$, then g is strictly convex.
- 2. Show that if f_1, \ldots, f_k are convex, then $g(x) = \max\{f_1(x), \ldots, f_k(x)\}$ is convex. Show that if all f_1, \ldots, f_k are convex, then g is strictly convex.
- 3. Assignment 2. Problem 1(a), (c), and (d)
- 4. Assignment 2. Problem 2. (For this one, figure out how to use Matlab to solve quadratic programming problems, i.e., problems of minimization of quadratic functionals subject to linear restrictions.)
- 5. Assignment 3. Problem 2(a) and (b)
- 6. Assignment 3, Problem 3.